BIG4: Biosystematics, informatics and genomics of the big 4 insect groups- training tomorrow's researchers and entrepreneurs

Kick-Off Meeting

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Copenhagen, Denmark

Statistical Phylogenetics

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Statistical Phylogenetics

- Despite the computational complexity, statistical approaches are becoming increasingly important in phylogenetics:
    - Difficult problems requiring accurate and unbiased inference (e.g., structure of rapid radiations)
    - More aspects of molecular evolution being examined (structural dependencies, positive selection etc)
    - Combination of background knowledge and sequence information (e.g., divergence time estimation)
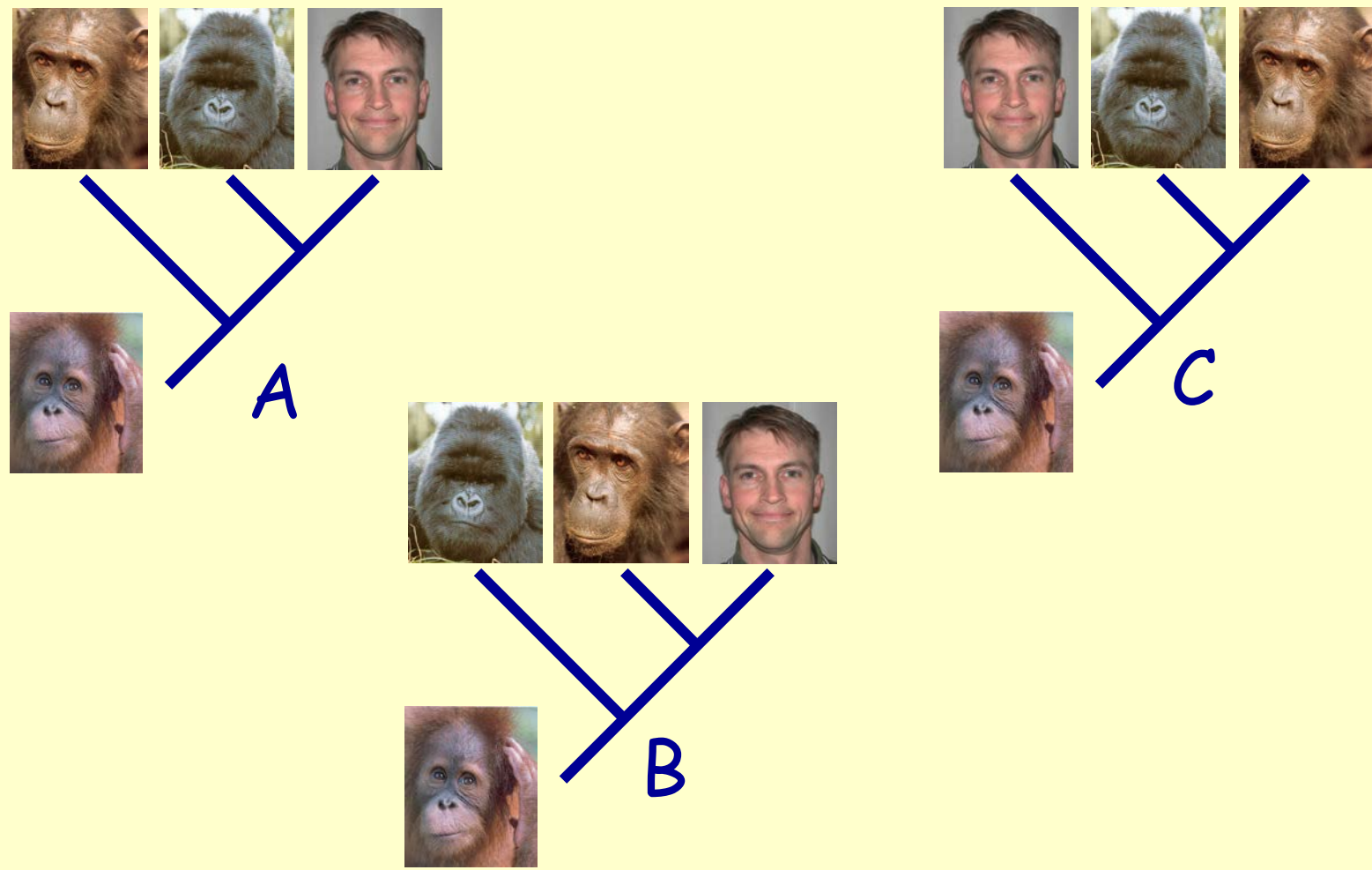   - Rich evolutionary models (e.g., biogeography)
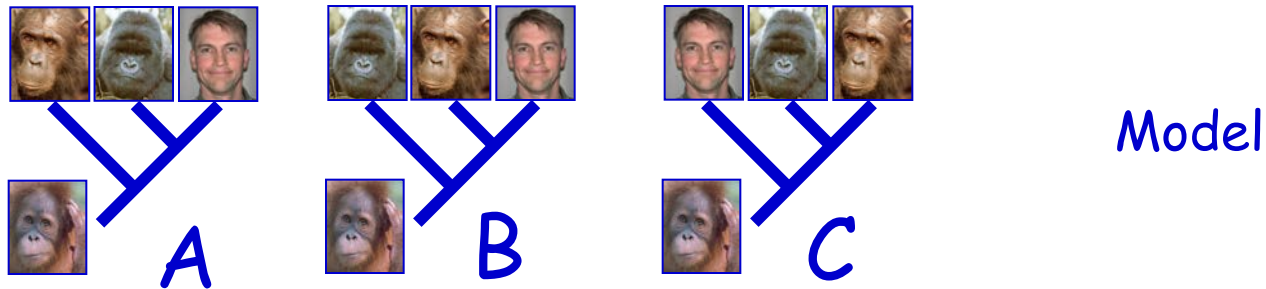
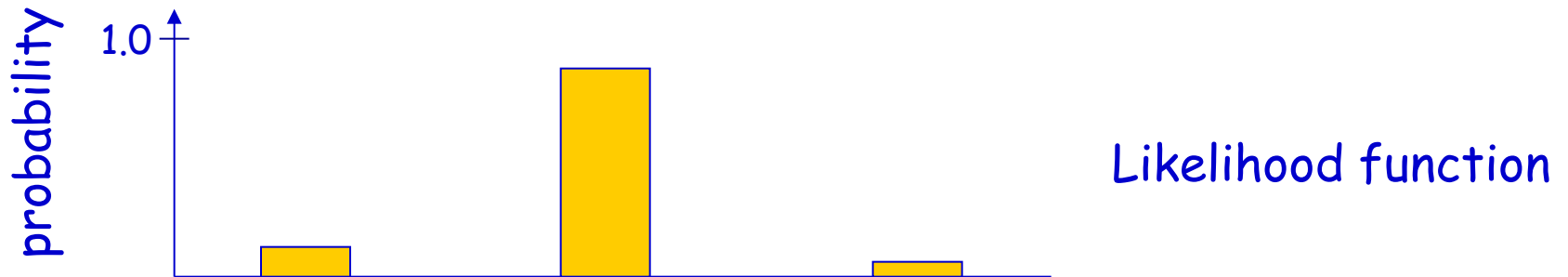# Infer relationships among three species:

Outgroup:

Three possible trees (topologies):

Maximum likelihood inference

Model

Data (observations)

probability

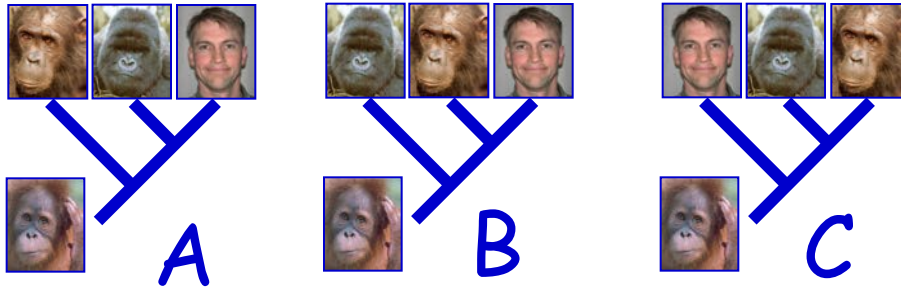1.0

Likelihood function

Bayesian inference

Model

Prior distribution

Data (observations)

Posterior distribution

Bayesian or ML?

- Maximum likelihood
  - Can be fast
  - Background knowledge ignored
  - No natural way of measuring uncertainty
  - Difficult to extend to complex models
  - Assessing quality of results from ML algorithms difficult
- Bayesian inference
  - May be slower
  - Possible to incorporate background knowledge
  - Natural measure of uncertainty (posterior probability distribution)
  - Standard computational machinery (Markov chain Monte Carlo), which can easily be extended to complex models
  - Convergence diagnostics for MCMC well developed

"My" Bayesian Software

- **MrBayes**
  - Large model space (but ~ fixed)
  - Robust and reliable
- **RevBayes**
  - Flexible model specification using graphical models concepts
  - Clunky but pretty competent
- **Rev**
  - Completely flexible graphical model specification
  - Programmable
  - Work in progress…

Software challenges

- Modeling explosion, especially in the Bayesian context
- Challenging for empiricists to communicate and correctly understand models
- Challenging for developers of inference software to cope with expanding model universe
- Addressed using switches and the like
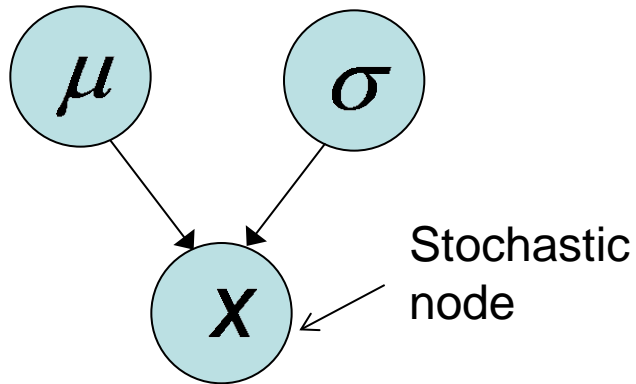- Can we develop more generic computational machinery?

Probabilistic Graphical Models

- Theoretical framework for specifying dependencies in complex statistical models
- Allows a complex model to be broken down into conditionally independent distributions
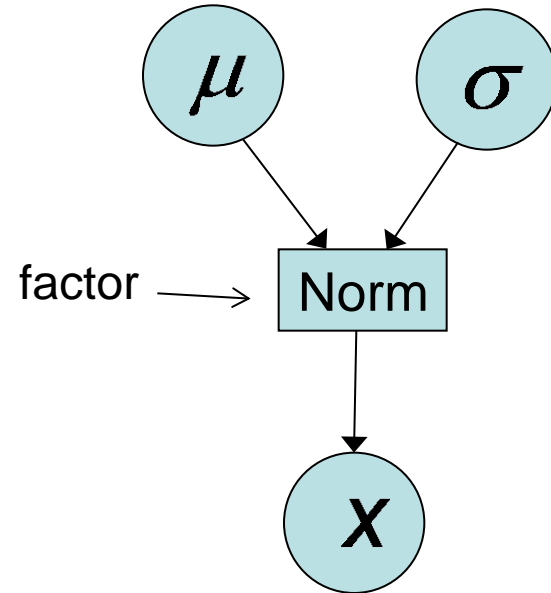- Closely related to standard statistical model formulae:

$$x \sim Norm(\mu, \sigma)$$

- Extensive literature on generic algorithms that apply to model graphs

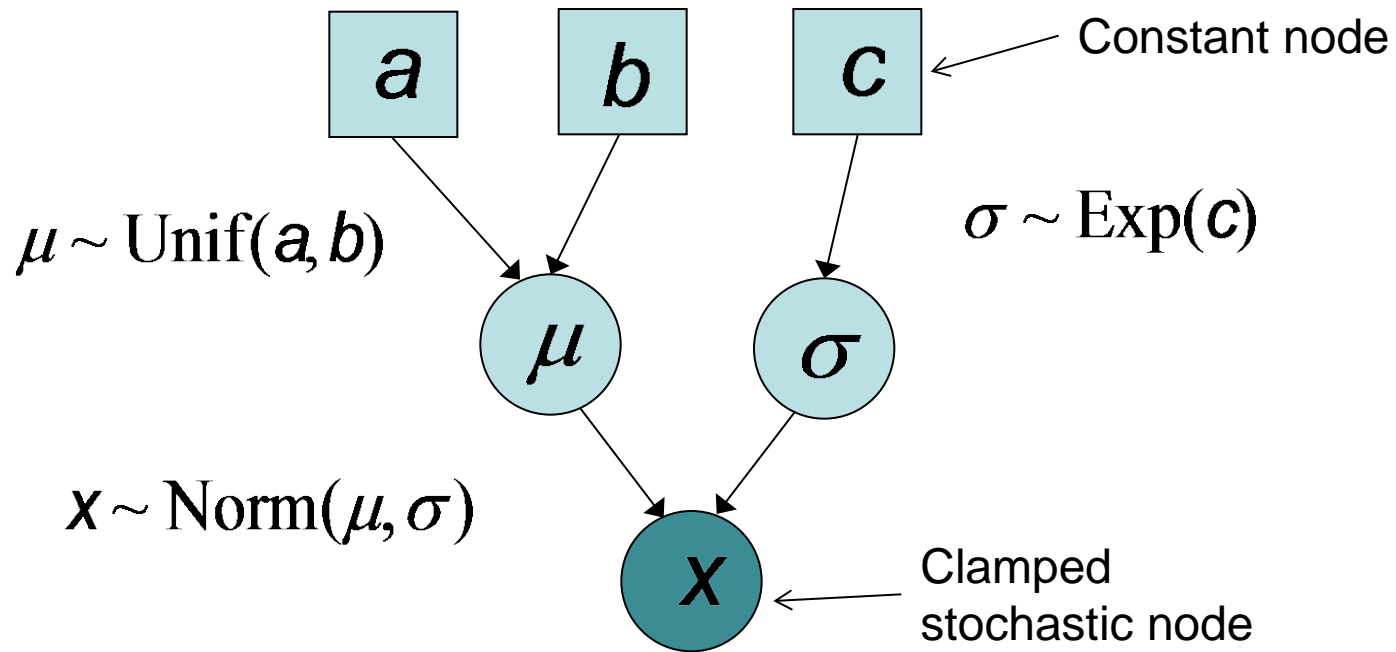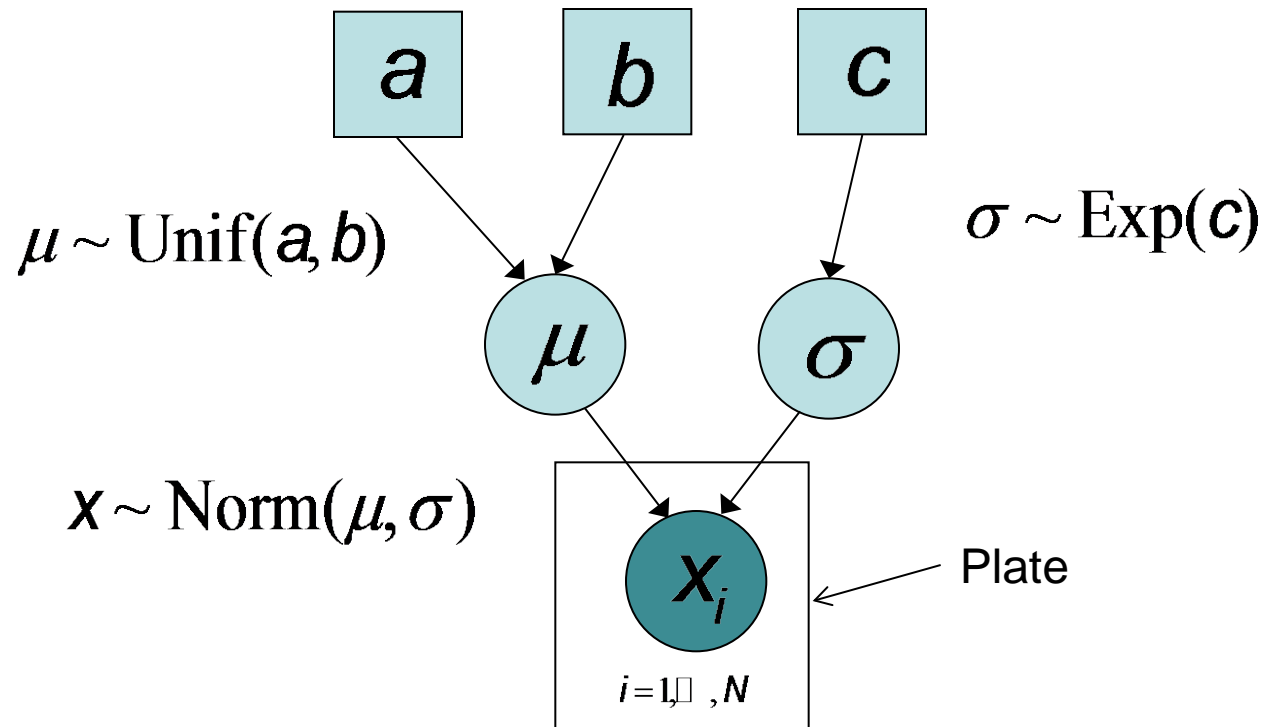$$x \sim \mathrm{Norm}(\mu, \sigma)$$

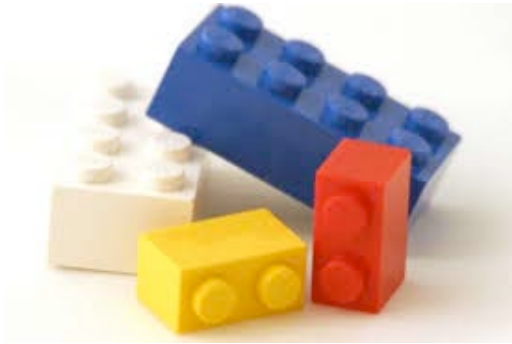Graphical Model
Compact Form

Factor Graph

Hierarchical Graphical Model

$\mu \sim \text{Unif}(a, b)$

$\sigma \sim \text{Exp}(c)$

$x \sim \text{Norm}(\mu, \sigma)$

Plate

$i = 1, \square, N$

RevBayes Project

- Interactive computing environment intended primarily for Bayesian phylogenetic inference
- Uses a special language, Rev, for constructing probabilistic phylogenetic and evolutionary graphical models interactively, step by step
- Rev is similar to R and the BUGS modeling language
- RevBayes provides generic computing machinery for simulation, inference and model testing

A complete MCMC analysis in Rev

```
a <- -1.0
b <- 1.0

mu    ~ dnUnif(a, b)
sigma ~ dnExp(1.0)

for (i in 1:10) {
   x[i] ~ dnNorm(mu, sigma)
   x[i].clamp(0.5)
}

mymodel = model(mu)   # Any stochastic node in the model works

mymcmc = mcmc(mymodel)

mymcmc.run(1000)
```

```
# definition of the myGTR function ("Ziheng's favorite")
function model myGTR (CharacterMatrix data) {

    # describe Q matrix
    pi ~ dflatdir(4);
    r  ~ dflatdir(6);
    Q := gtr(pi, r);

    # describe tree
    tau ~ dtopuni(data.taxa(), rooted=false);

    # gamma shape
    alpha ~ dunif(0.0, 50.0);

    # discrete gamma mixture
    for (i in 1:4)
        catRate[i] := qgamma(i*0.25-0.125, alpha, alpha);
    for (i in 1:data.size())
        ratecat[i] ~ dcat(simplex(0.25,0.25,0.25,0.25));

    # associate distributions with tree parts
    for (i in 1:data.size()) {
        for (n in 1:tau.numNodes()) {
            if (tau.isTerminal(n)) {
                tau.length[n] ~ exp(1.0);
                tau.state[n] ~ ctmc(Q, e.length*catRate[ratecat[i]],
                    tau.state[tau.parent(n)]);
                tau.state[n] <- data[i][tau.tipIndex(n)];
            }
            else {
                tau.length[n] ~ exp(10.0);
                tau.state[n] ~ ctmc(Q, e.length*catRate[ratecat[i]],
                    tau.state[n]);
            }
        }
    }

    # return model
    return model( Q );
}
```

Definition of a new phylogenetic model

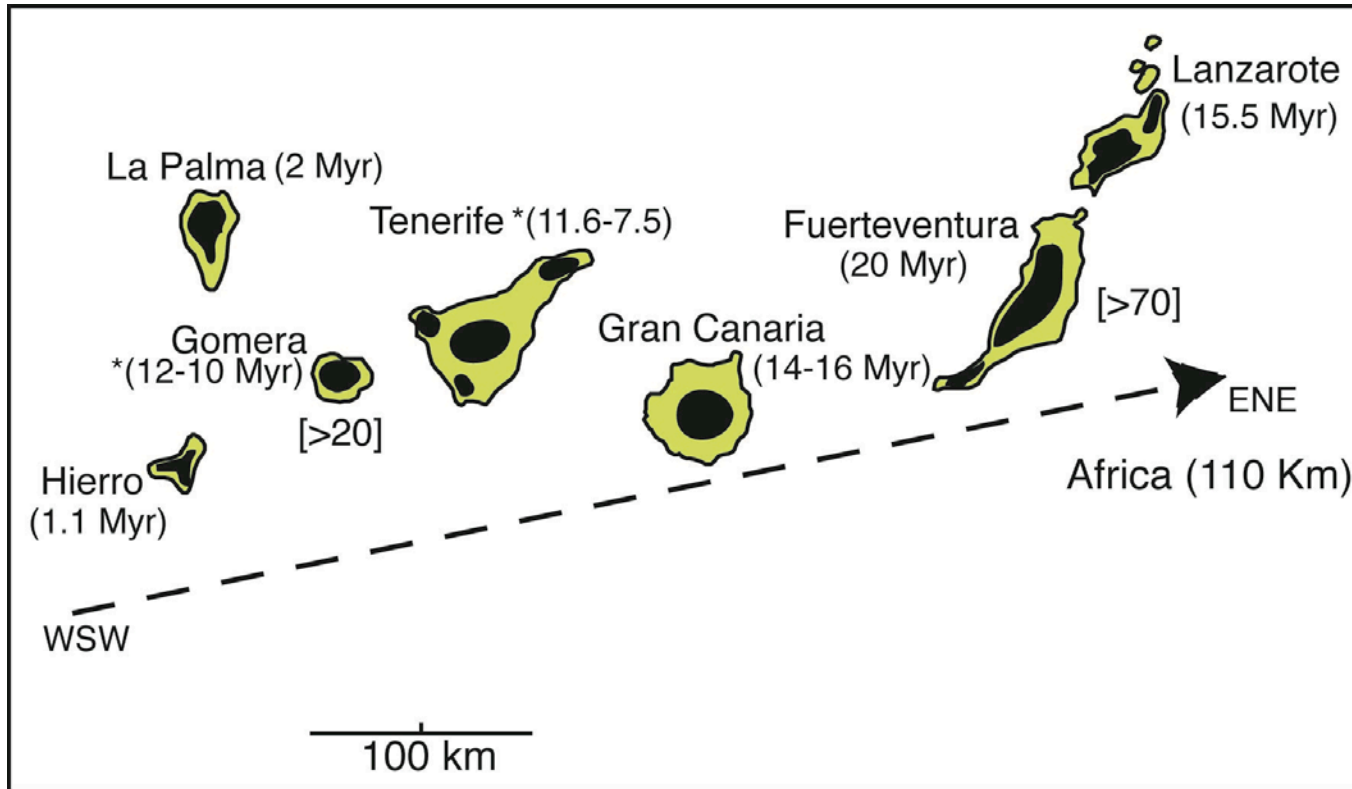Appr. 20 lines

Complexity hidden from normal user

```
# Read in data
myData <- read( "data.nex" )

# Apply model
myModel = zihengGTR( myData )

# Construct mcmc
myMCMC = mcmc( myModel )

# Run mcmc
myMCMC.run(10000)
```
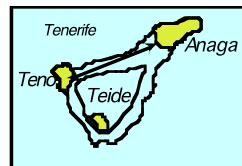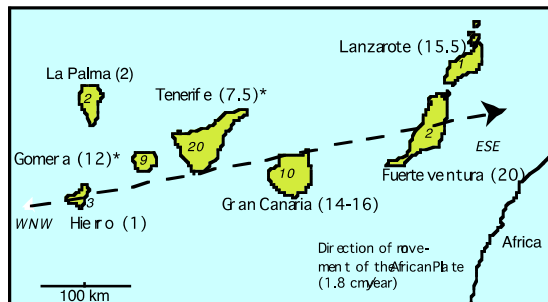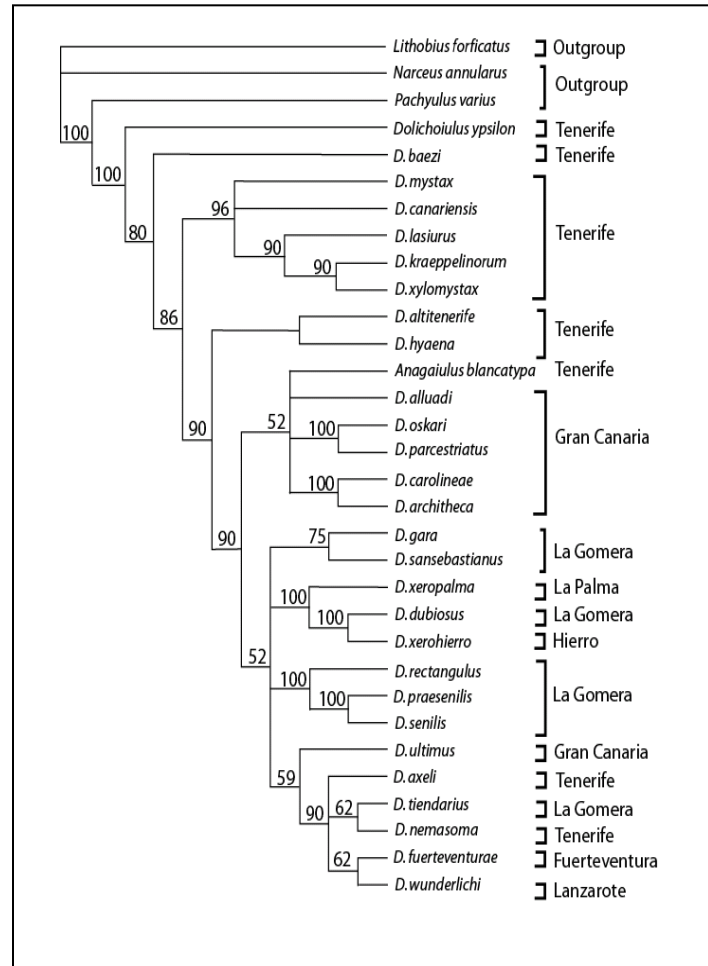
The Canary Islands

Dolichoiulus (Diplopoda)

Dolichoiulus (Diplopoda, Julida, Julidae, Pachyulinae)

46 endemic species

Model

Organism groups

distribution

T_1	DNA data 1 — GTR_1 — μ_1	m_1
T_2	DNA data 2 — GTR_2 — μ_2	m_2
T_3	DNA data 3 — GTR_3 — μ_3	m_3

IM

IM – island model
μ_i – mutation rate
m_i - dispersal rate

Inference

Bayesian inference using MCMC sampling,
accommodating uncertainty in all model parameters

Canary Islands: 3-island model

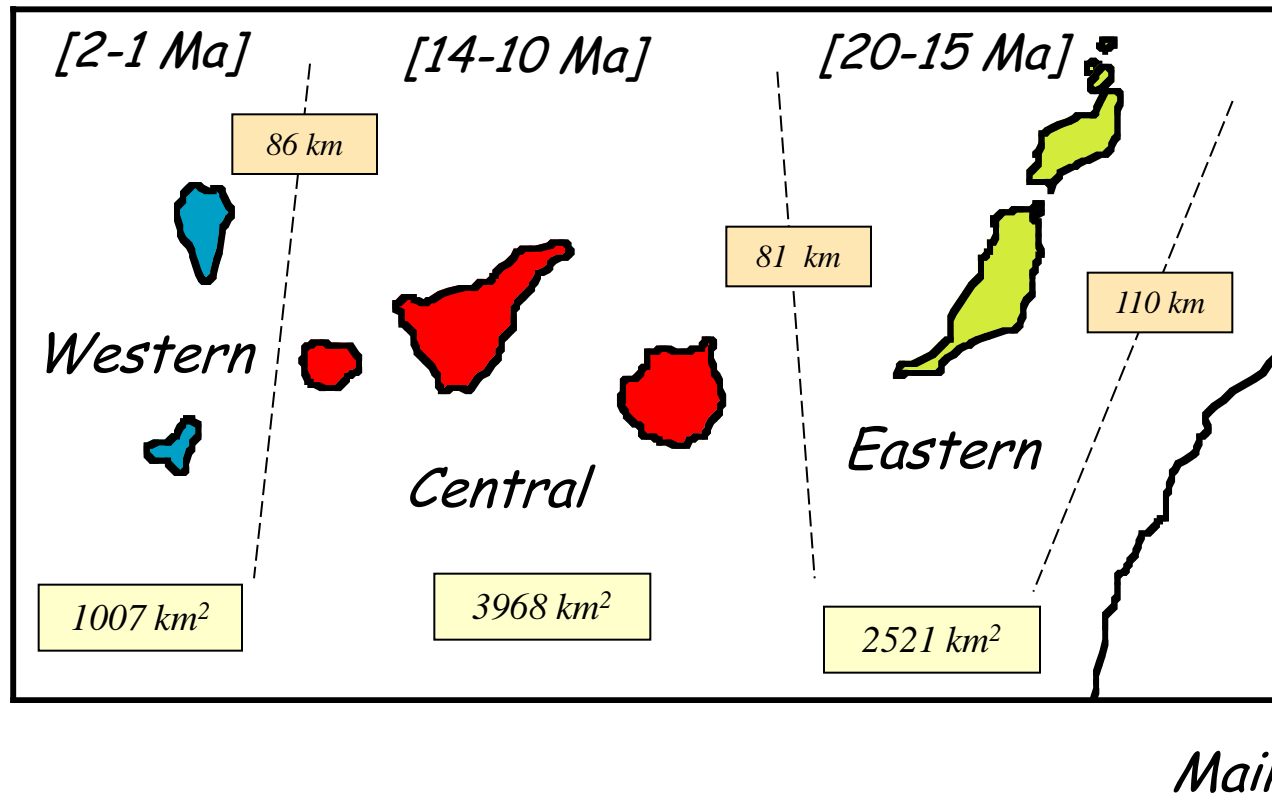[2-1 Ma]   [14-10 Ma]   [20-15 Ma]

86 km

Western

81 km

110 km

Eastern

Central

1007 km²   3968 km²   2521 km²

Mainland

Ecological zones

- Coastal belt
- Open habitat
- Thermophilous forest
- Laurisilva
- Pine forest
- Sub-alpine

Ten island–habitat types

M1	Other Mainland
E2	Eastern-Open
C2	Central-Open
W2	Western Open
C3	Central-laurel forest
W3	Western-laurel forest
C4	Central-pine forest
W4	Western-pine forest
C5	Central-alpine vegetation
W5	Western-alpine vegetation

Zona de Cumbre
Zona de Pinar
Zona de Laurisilva
Zona Bosque Termófilo
Zona Litoral
Zona Baja

L. Martinez 2010

Separating island-hopping and niche-shift rates

$$r \begin{cases} r_i & \text{Shift between islands} \\ r_e & \text{Shift between niches} \\ r_i r_e & \text{Shift between islands and niches} \end{cases}$$

Standard biogeography model:

r ~ dirichlet(1, 1, 1, ...)

Islands-ecology model:

mu ~ dirichlet(1, 1)

r := simplex(mu[1], mu[2], mu[1] * mu[2], ...)